

MEB, Department Seminar, November 9, 2007



**Karolinska  
Institutet**

# **Sensitivity to Change of Outcome Measures**

Wilmar Igl

Psychologist, PhD

Department of Medical Epidemiology and Biostatistics

Karolinska Institutet

# Introduction (I)

- **Measurement of change** is frequently applied in clinical research.
- Effects of health changes depend not only on the intervention, but also on the quality of the applied **measurement tools**.
- **Categories of measurement goals** (Kirshner & Guyatt, 1985):
  - Discrimination, e.g. between groups with different morbidity
  - Prognosis, e.g. prediction of treatment success
  - Evaluation, e.g. changes caused by interventions
- Regarding **evaluation studies** sensitivity to change is of primary importance.
- **Sensitivity to change/Responsiveness**:  
The ability of an instrument to measure change.

## Introduction (II)

**Weighing machine** with a measurement error of  $\pm 3$  kg (Norman, 1989):

- Individuals with 60 to 150 kg initial weight
- Intervention with an average weight reduction of 2 kg/week

**Sickness Impact Profile** (SIP, Bergner et al., 1981)

- Question: "Have you ever attempted suicide?"
- Answer:  yes  no

These measurement tools seem ...

- **adequate** for differentiating between groups (discrimination)
- **inadequate** for measuring change caused by a interventions (evaluation)

# I. Theoretical Background

# What is a (good) Test?

- **Definition** (cf. Rost, 2004):  
*"A test is a special (psychological) experiment to compare individuals (or groups) and/or items (or aggregated scores)."*

- Derivation of test criteria from the **general theory of measurement error** (cf. classical test theory):

$$X = T + E$$

- **Reliability** (cf. "precision"):

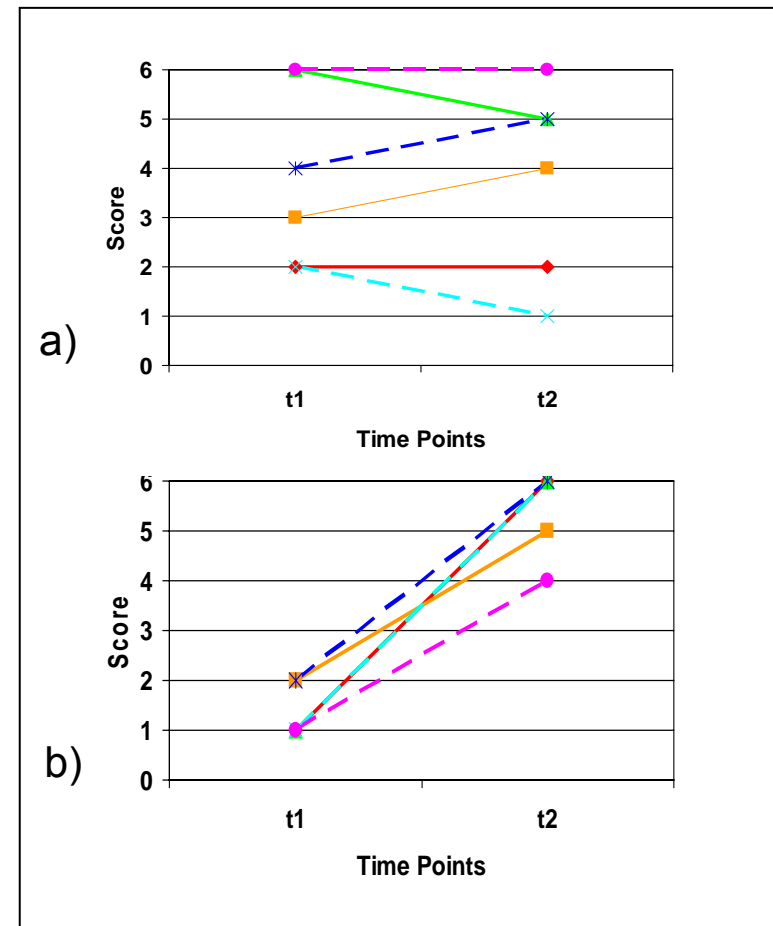
$$Rel = \frac{\sigma^2(T)}{\sigma^2(X)}$$

- **Validity** (cf. "unbiasedness"):

$$Val = \frac{cov(T, C)}{\sigma(T) \cdot \sigma(C)}$$

# Correlational vs. Experimental Approach

- Different methods to measure test criteria are necessary for the measurement of state vs. the measurement of change (cf. Cronbach, 1957).
- **Correlational approach:**  
(cf. measurement of state)
  - *Inter*-individual differences as "signal"
  - *Intra*-individual change as "noise"
- **Experimental approach:**  
(cf. measurement of change)
  - *Inter*-individual differences as "noise"
  - *Intra*-individual change as "signal"



# Measurement of state: Methods

- **Methods for measuring reliability:**
  - Test-retest reliability
  - Parallel-test reliability
  - Split-half reliability
  - Internal consistency
  
- **Methods for measuring validity:**
  - Criterion validity (e.g. via a valid reference standard)
  - Construct validity (e.g. via *Multitrait-Multimethod-approach*, Campbell & Fiske, '59)

These methods are usually based on correlational methods!

They are not appropriate for the measurement of (homogenous) change!

# Data Example

Measurement	Instrument	Subject	t1	t2	t2-t1	r(tt)	r(tc, t1)	ES=m/sd
State	Test	1	2	2	0	0.89	0.96	0,00
	Test	2	3	4	+1			
	Test	3	6	5	-1			
	Criterion	1	2	1	-1	0.94		0,00
	Criterion	2	4	5	+1			
	Criterion	3	6	6	0			
Measurement	Instrument	Subject	t1	t2	t2-t1	r(dd)	r(tc, t2-t1)	ES=m/sd
Change	Test	1	1	6	5	NA	0,00	3,75
	Test	2	2	5	3			
	Test	3	1	6	5			
	Criterion	1	1	6	5	NA		4,00
	Criterion	2	2	6	4			
	Criterion	3	1	4	3			



# Data Example

Measurement	Instrument	Subject	t1	t2	t2-t1	r(tt)	r(tc, t1)	ES=m/sd
State	Test	1	2	2	0	0.89	0.96	0,00
	Test	2	3	4	+1			
	Test	3	6	5	-1			
	Criterion	1	2	1	-1	0.94		0,00
	Criterion	2	4	5	+1			
	Criterion	3	6	6	0			
Measurement	Instrument	Subject	t1	t2	t2-t1	r(dd)	r(tc, t2-t1)	ES=m/sd
Change	Test	1	1	6	5	NA	0,00	3,75
	Test	2	2	5	3			
	Test	3	1	6	5			
	Criterion	1	1	6	5	NA		4,00
	Criterion	2	2	6	4			
	Criterion	3	1	4	3			

# Data Example

Measurement	Instrument	Subject	t1	t2	t2-t1	r(tt)	r(tc, t1)	ES=m/sd
State	Test	1	2	2	0	0.89	0.96	0,00
	Test	2	3	4	+1			
	Test	3	6	5	-1			
	Criterion	1	2	1	-1	0.94		0,00
	Criterion	2	4	5	+1			
	Criterion	3	6	6	0			
Measurement	Instrument	Subject	t1	t2	t2-t1	r(dd)	r(tc, t2-t1)	ES=m/sd
Change	Test	1	1	6	5	NA	0,00	3,75
	Test	2	2	5	3			
	Test	3	1	6	5			
	Criterion	1	1	6	5	NA		4,00
	Criterion	2	2	6	4			
	Criterion	3	1	4	3			

# Data Example

	Measurement	Instrument	Subject	t1	t2	t2-t1	r(tt)	r(tc, t1)	ES=m/sd
State	Test		1	2	2	0	0.89	0.96	0,00
	Test		2	3	4	+1			
	Test		3	6	5	-1			
	Criterion		1	2	1	-1	0.94		0,00
	Criterion		2	4	5	+1			
	Criterion		3	6	6	0			
	Measurement	Instrument	Subject	t1	t2	t2-t1	r(dd)	r(tc, t2-t1)	ES=m/sd
Change	Test		1	1	6	5	NA	0,00	3,75
	Test		2	2	5	3			
	Test		3	1	6	5			
	Criterion		1	1	6	5	NA		4,00
	Criterion		2	2	6	4			
	Criterion		3	1	4	3			

# Data Example

	Measurement	Instrument	Subject	t1	t2	t2-t1	r(tt)	r(tc, t1)	ES=m/sd
State	Test		1	2	2	0	0.89	0.96	0,00
	Test		2	3	4	+1			
	Test		3	6	5	-1			
	Criterion		1	2	1	-1	0.94		0,00
	Criterion		2	4	5	+1			
	Criterion		3	6	6	0			
	Measurement	Instrument	Subject	t1	t2	t2-t1	r(dd)	r(tc, t2-t1)	ES=m/sd
Change	Test		1	1	6	5	NA	0,00	3,75
	Test		2	2	5	3			
	Test		3	1	6	5			
	Criterion		1	1	6	5	NA		4,00
	Criterion		2	2	6	4			
	Criterion		3	1	4	3			

# Measurement of Change: Methods

- **Definition:**  
„Sensitivity to change is defined as the ability of an instrument to measure "true" change of a latent construct.“
- **Synonyms:** responsiveness, longitudinale validity, evaluative validity
- **At present:**  
*Controversial discussion of different definitions and methods  
(25 definitions, 31 coefficients/designs, Terwee et al., 2003)*
- **Theoretical categories (Terwee et al., 2003):**
  - a) *Ability to measure change in general*
  - b) *Ability to measure clinical significant change*
  - c) *Ability to measure change of a construct of interest*

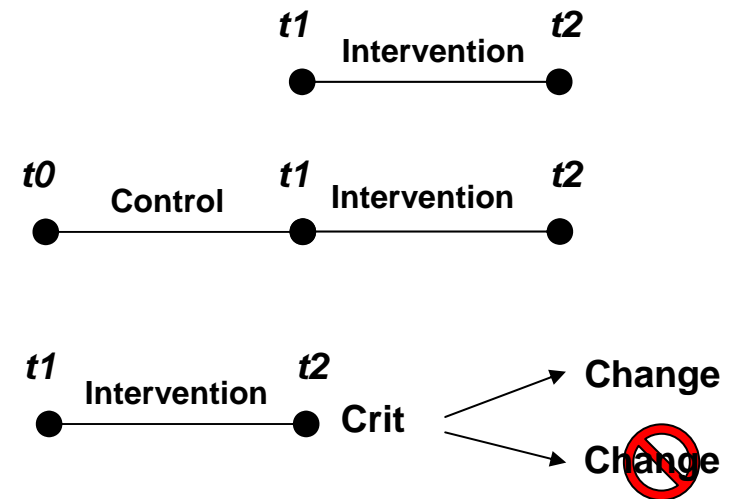
# Study Designs

- Single-group designs

  - simple pre-post design

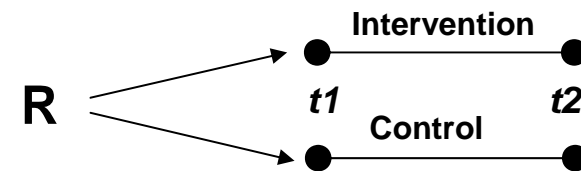
  - pre-post design with baseline

  - simple pre-post design with external criteria



- Two-group designs

  - (with intervention and control group)



# Coefficients

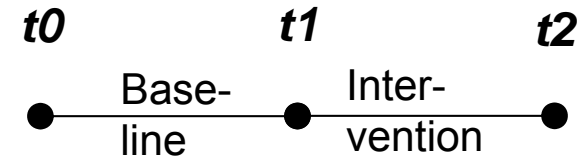
- **Criterion-based coefficients**

- Pearson correlation  $r$
- Linear regression
- AUC (ROC analysis)

- **Distribution-based coefficients**

- Statistical tests ( $t$ - ,  $F$ - ,  $p$ -values)
- Norman's coefficients  $S_{ANOVA}$  and  $S_{ANCOVA}$
- Standardized effect sizes:
  - easy to calculate
  - not dependent on sample size
  - widespread application
  - ... but interpretation depends on specific design and formula

# Standardized Effect Sizes



$$SES = \frac{m(t_2) - m(t_1)}{s(t_1)}$$

- SD of values  $x(t_1)$  at the **beginning of intervention**
- high values if variability is small

$$SRM = \frac{m(t_2) - m(t_1)}{s(t_2 - t_1)}$$

- SD of the difference  $x(t_2) - x(t_1)$  of the **intervention interval**
- high values if variability of differences  $x(t_2) - x(t_1)$  is small

$$GRI = \frac{m(t_2) - m(t_1)}{s(t_1 - t_0)}$$

- SD of differences  $x(t_1) - x(t_0)$  of the **baseline interval**
- high values if variability of differences  $x(t_1) - x(t_0)$  is small
- measuring/confounding change and stability



# Using Controlled Trials to Compare Measurement Tools



- Expenditures for clinical trials could be minimized by using better measurement tools.
- Comparative studies to select the best instruments are necessary.
- Designs applying multiple instruments on the same sample are most useful.
- Instruments can be evaluated using descriptive coefficients.
- Sampling error has to be taken into account by calculating confidence intervals or using hypothesis tests.

## II. A prospective, comparative study

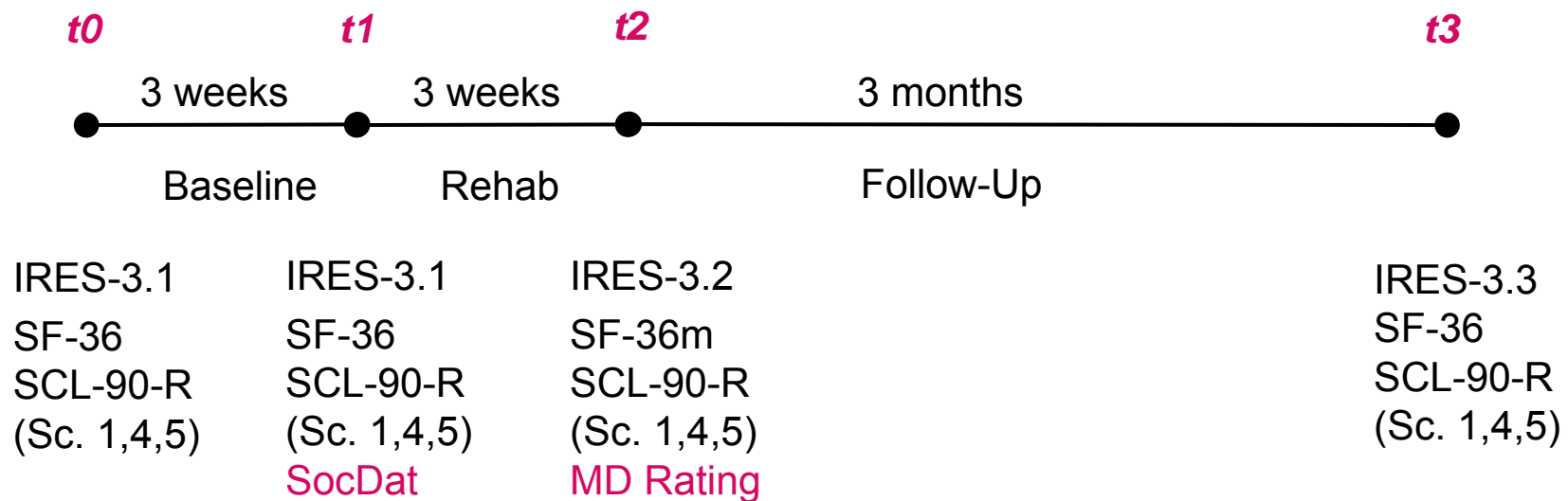
Igl, W., Zwingmann, C. & Faller, H. (2006). Änderungssensivität von Fragebogen zur Erfassung der subjektiven Gesundheit – Ergebnisse einer prospektiven vergleichenden Studie [Sensitivity to change of questionnaires measuring subjective health - results of a prospective comparative study]. *Rehabilitation* 45(4), 232-242.

# Sample

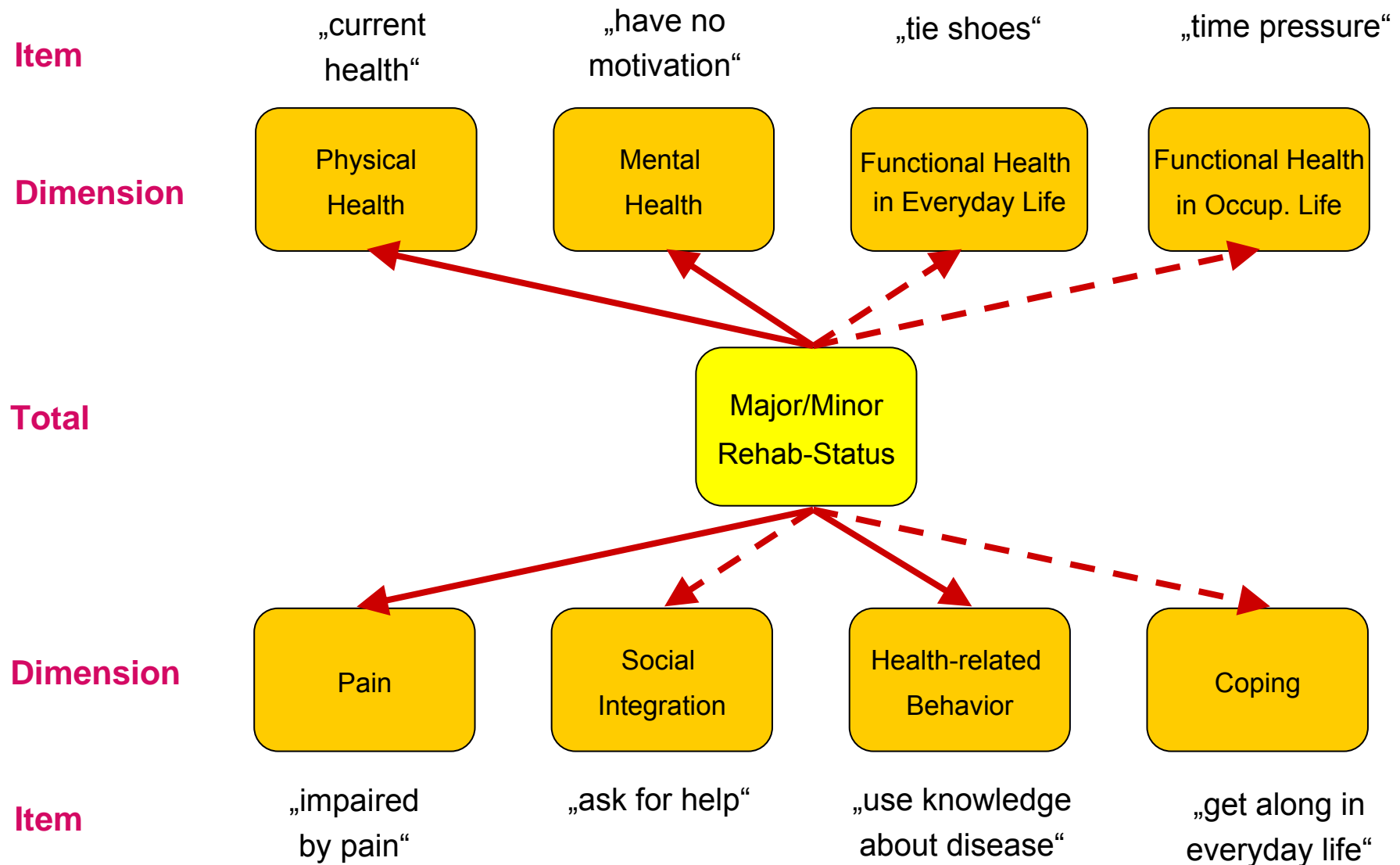
	<b>Total</b>	<b>Orthopedic/ rheumatic Rehabilitation</b>	<b>Cardiac Rehabilitation</b>
<b>N(Participants)</b>	1145 (100%)	745 (65%)	400 (35%)
<b>Sex</b>	N(F) = 42% N(M) = 58%	N(F) = 53% N(M) = 47%	N(F) = 22% N(M) = 78%
<b>Age</b>	M = 50 years SD = 8.6 years	M = 49 years SD = 8.9 years	M = 51 years SD = 7.9 years

# Sample and Study Design (I)

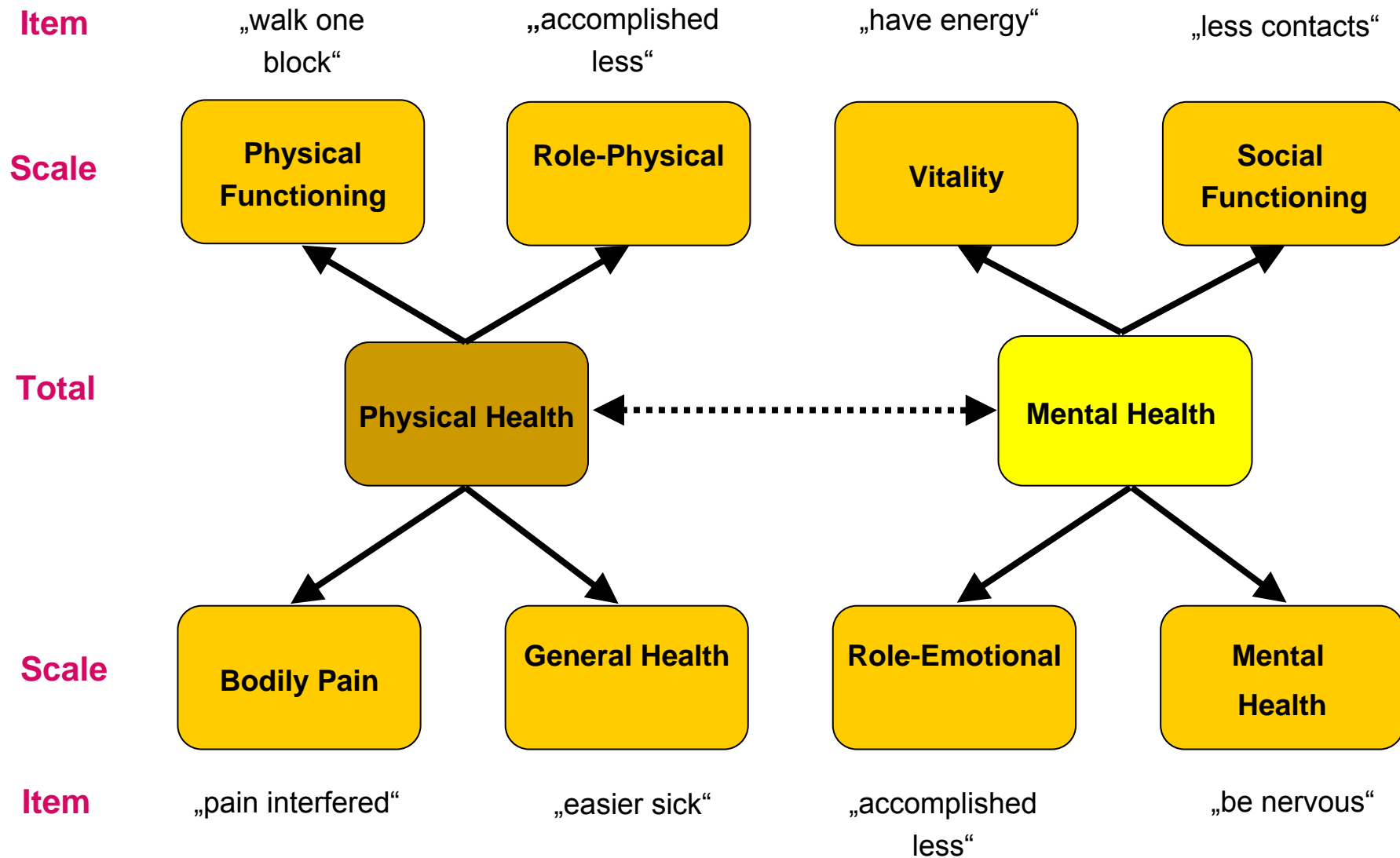
- **Sample:**
  - N = 745 patients, orthopedics/rheumatology (ICD, M00-M99),
  - N = 400 patients, cardiology (ICD, I00-I99)
- **Treatment:** „Medical Rehabilitation“ (usual care)
- **Prospective, comparative one-group design:**



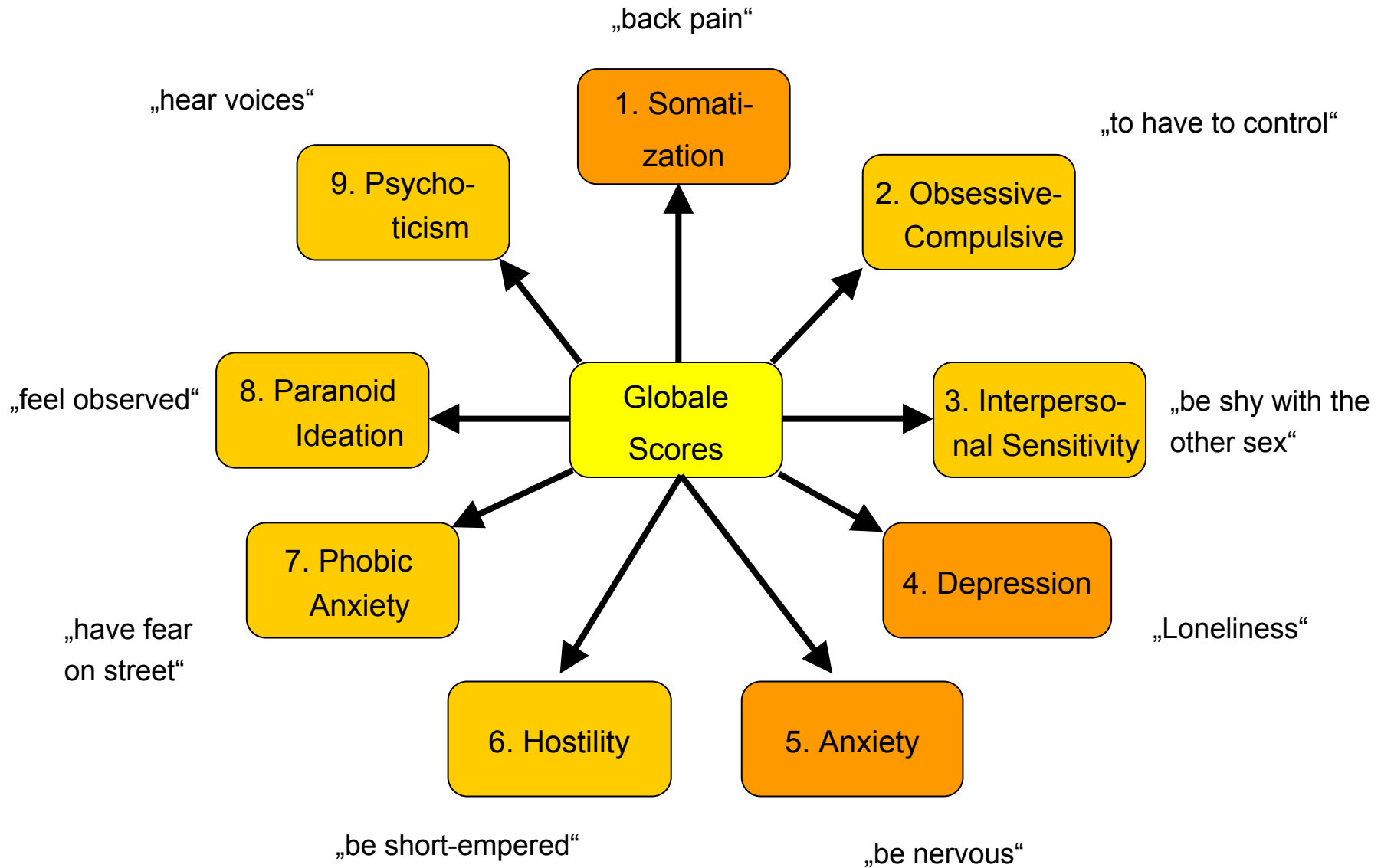
# IRES-3\* – Measurement Model (scales omitted)



# SF-36\* – Measurement Model



# SCL-90-R\* – Measurement Model



# Study Design (II)

- **Independent Variables:**
  - 1st factor: Interventions (baseline, usual care, follow-up)
  - 2nd factor: Measurement instruments (IRES-3, SF-36, SCL-90-R (1, 4,5), Health-related quality of life (HRQOL) questionnaires)
  
- **Dependent Variables:**
  - 1st end point: Coefficients of sensitivity to change (SRM)
  - 2nd end point: Coefficients of stability ( $r_{tt}$ , Cronbach's  $\alpha$ )
  
- **Confounding Variables:**
  - Sequence of questionnaires: complete permutation (ABC, ACB, ..., CBA)
  - Sequence of interventions: not controlled (only empirically!)
  - Different constructs: theoretical (cross-person model of health-related quality of life) and empirical (principal component analysis) matching of scores



# Statistical analysis

- **Separate analysis** according to diagnosis, measurement intervals, constructs and aggregation levels of scores
- **Descriptive evaluation of coefficients** based on the distribution of coefficients per diagnostic group and measurement interval
- **Sensitivity to change beyond error:**  
Estimation of confidence intervals (95%, 2-sided) of SRM coefficients based on non-central  $t$ -distributions (Smithson, 2002).
- **Relative sensitivity to change:**  
Estimation of confidence intervals (99%, 2-sided) of *differences of SRM* coefficients based on resampling methods (Hesterberg et al., 2005).

# Principal Components Analysis

- **Principal Components Analysis** (PCA) including scores of all questionnaires (Varimax rotation, available case approach, Eigen values > 1)
  - Similar factor solutions in both diagnostic groups
  - Score correlate with the expected factors in most cases
- **Principal Component Analysis I** (IRES-3 dimensions, no IRES-3 scales):
  - 19 scores, N = [299;626]
  - 2 factors: "Psyche", "Soma" (Var(explained, per factor)  $\approx$  30% per Factor)
  - Variance(explained, total)  $\approx$  62%
- **Principal Component Analysis II** (IRES-3 scales, no IRES-3 dimensions):
  - 38 scales, N = [297;626]
  - 6 factors: "Psyche", "Pain", "EverydayLife", "Social", "Behavior", "Job"  
(Var(explained, per factor) < 19%)
  - Variance(explained, total)  $\approx$  65%

# Analysis of Coefficients

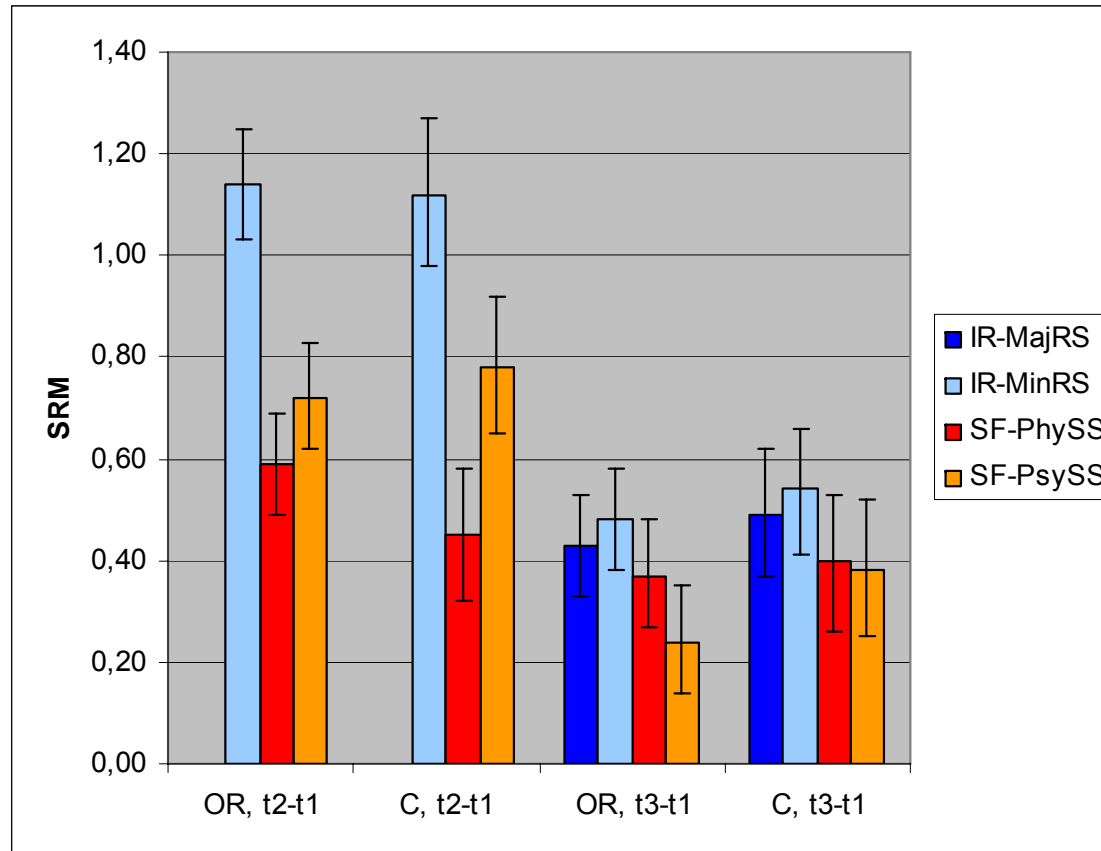
Comparison of effect sizes (SES, SRM, GRI):

- Substantial differences in means:  $M(\text{SES}) < M(\text{SRM}) \ll M(\text{GRI})$
- Partially differences in standard deviation:  $\text{SD}(\text{SES}) \approx \text{SD}(\text{SRM}) < \text{SD}(\text{GRI})$
- high correlations:  $r > 0.90$

*Table:* Descriptive Evaluation of SRM coefficients in categories

		SRM		
	Diagnosis	"small"	"medium"	"large"
Admission to Discharge	OR/K	[0.00;0.35]	[0.35;0.70]	[0.70;1.05]
Admission to Follow-Up	OR K	[0.00;0.16] [0.00;0.20]	[0.16;0.33] [0.20;0.40]	[0.33;0.49] [0.40;0.60]
<b>Cohen's <i>d</i></b>		0.2	0.5	0.8

# General Health (I)



*Fig. 1:* Sensitivity to change beyond chance of Scores of "General Health" (SRM, 95%-CIs)

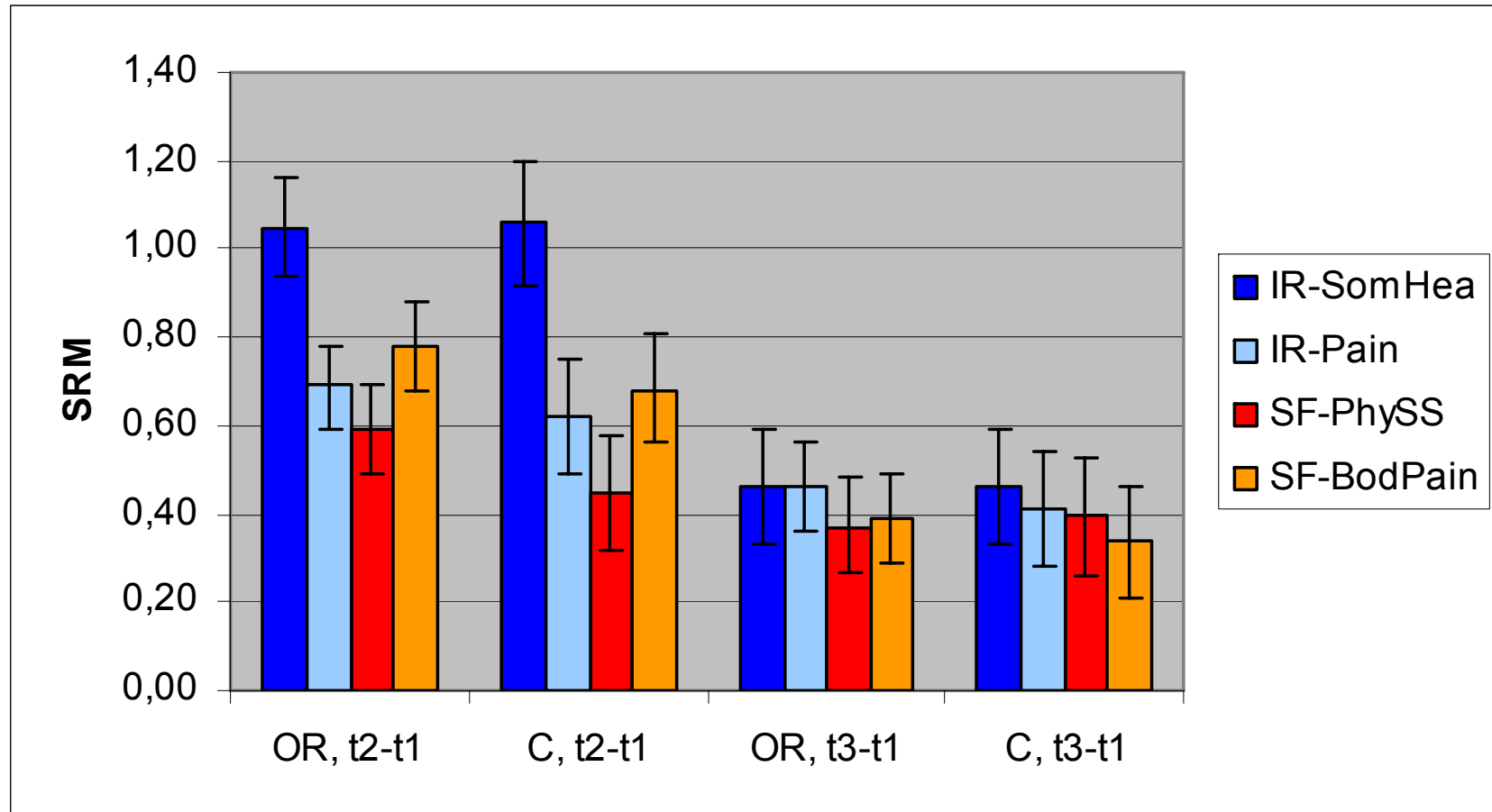
# General Health (II)

Table 1: Relative Sensitivity to change (SRM differences) of "General Health" scores

SCORES	Orthopedics/Rheumatology			Cardiology		
	IRES3 – SF36 (SRM)	DIFF (SRM)	DIFF <sub>Res</sub>	IRES3 – SF36 (SRM)	DIFF (SRM)	DIFF <sub>Res</sub>
<b>Admission to Discharge</b>						
MinRS – PhysHea	1.14 – 0.59	<b>0.55**</b> [0.43;0.72]	0.58	1.12 – 0.45	<b>0.69**</b> [0.43;0.91]	0.67
KleinRS – MentHea	1.14 – 0.72	<b>0.42**</b> [0.29;0.59]	0.44	1.12 – 0.78	<b>0.34**</b> [0.16;0.61]	0.38
<b>Admission to Follow-Up</b>						
MajRS – PhysSS	0.49 – 0.38	<b>0.06 (ns)</b> [-0.07;0.19]	0.06	0.49 – 0.40	<b>0.09 (ns)</b> [-0.05;0.27]	0.11
MajRS – MentHea	0.43 – 0.24	<b>0.19**</b> [0.10;0.37]	0.23	0.49 – 0.38	<b>0.11 (ns)</b> [-0.02;0.31]	0.15

Note: ns = not significant, 99%-CIs in squared brackets

# Somatic Health/Pain (I)



*Fig. 2:* Sensitivity to change beyond error of scores indicating "Somatic Health"/"Pain" (SRM, 95%-CIs)

## Physical Health/Pain (II)

Table 2: Relative sensitivity to change (SRM differences) of scores measuring "Physical Health" / "Pain"

SCORES	Orthopedics/Rheumatology			Cardiology		
	IRES3 – SF36 (SRM)	DIFF (SRM)	DIFF <sub>Res</sub>	IRES3 – SF36 (SRM)	DIFF (SRM)	DIFF <sub>Res</sub>
<b>Admission to Discharge</b>						
SomHea – PhyHea	1.05 – 0.59	<b>0.46**</b> [0.33;0.62]	0.47	1.06 – 0.45	<b>0.61**</b> [0.39;0.83]	0.60
Pain – BodPain	0.69 – 0.78	<b>- 0.09 (ns)</b> [-0.22;0.01]	-0.11	0.62 – 0.68	<b>- 0.06 (ns)</b> [-0.25;0.08]	-0.08
<b>Admission to Follow-Up</b>						
SomHea – PhyHea	0.46 – 0.37	<b>0.09 (ns)</b> [-0.04;0.21]	0.09	0.46 – 0.40	<b>0.06 (ns)</b> [-0.07;0.26]	0.09
Pain– BodPain	0.46 – 0.39	<b>0.07 (ns)</b> [-0.12;0.09]	-0.01	0.41 – 0.34	<b>0.07 (ns)</b> [-0.09;0.21]	0.06

Note: ns = not significant, 99%-CIs in squared brackets

# Mental Health (I)

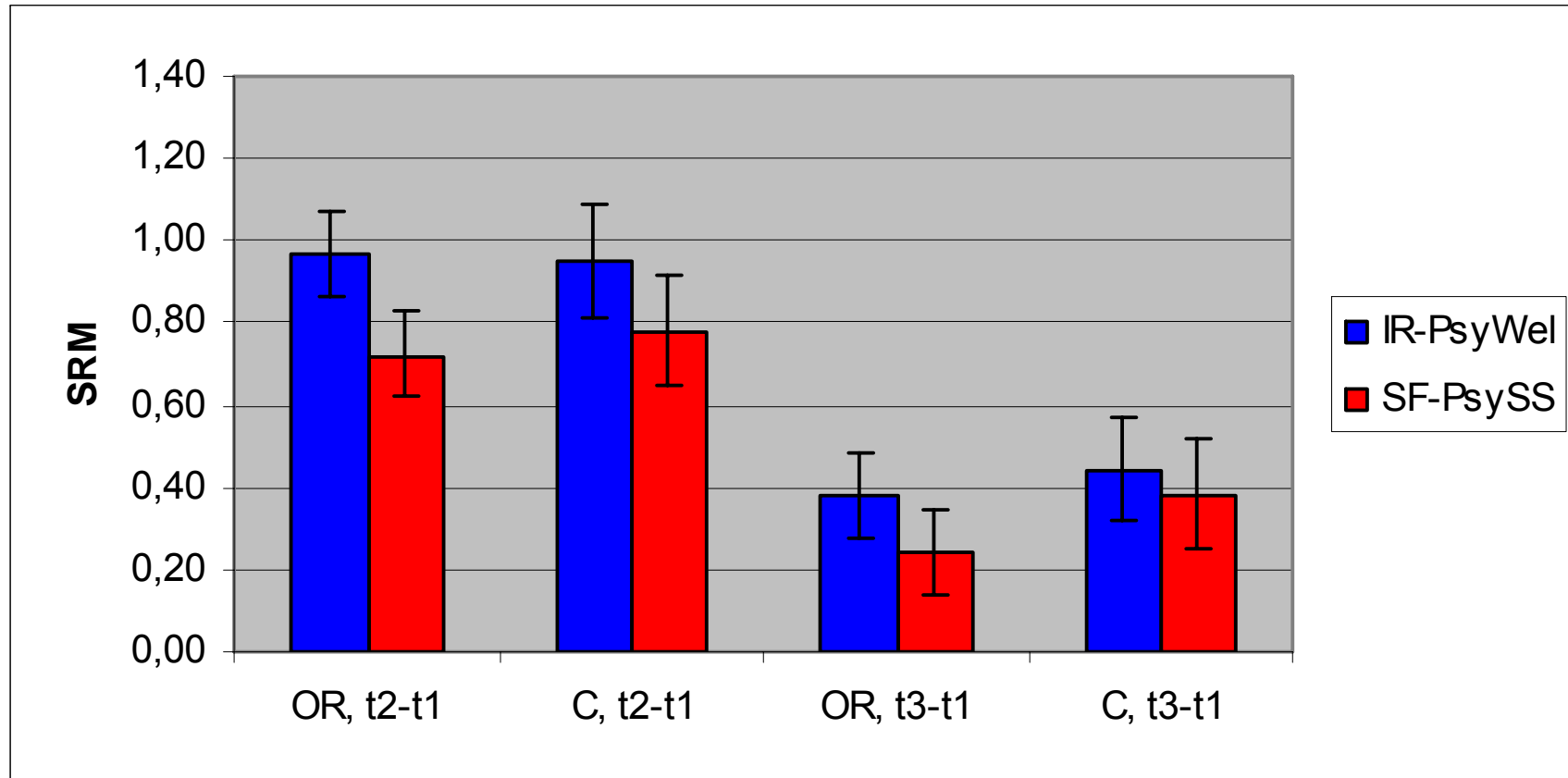


Fig. 3: Sensitivity to change beyond error of scores measuring "Mental Health" (SRM, 95%-KIs)



## Mental Health (II)

Table 3: Relative sensitivity to change (SRM differences) of scores measuring "Mental Health"

	Orthopedics/Rheumatology			Cardiology		
SCORES	IRES3 – SF36 (SRM)	DIFF (SRM)	DIFF <sub>Res</sub>	IRES3 – SF36 (SRM)	DIFF (SRM)	DIFF <sub>Res</sub>
<b>Admission to Discharge</b>						
PsyWel – MentHea	0.97 – 0.72	<b>0.25**</b> [0.15;0.42]	0.28	0.95 – 0.78	<b>0.17**</b> [0.04;0.40]	0.21
<b>Admission to Follow-Up</b>						
PsyWel – MentHea	0.38 – 0.24	<b>0.14**</b> [0.07;0.30]	0.19	0.44 – 0.38	<b>0.06 (ns)</b> [-0.06;0.26]	0.10

Note: ns = not significant, 99%-CIs in squared brackets

## III. Summary and Conclusion

# Sensitivity to Change and Sample Size

Construct	Rehabilitation Admission to Discharge (3 Wks.)		Rehabilitation Admission to Follow-Up (3 Mts.)	
	Orthopedics/ Rheumatology	Cardiology	Orthopedics/ Rheumatology	Cardiology
<b>General Health</b>	IRES-3 (9:18,9:25)	IRES-3 (9:15, 9:41)	IRES-3 (45:139, 45:60)	IRES-3 (35:60, 35:52)
<b>Physical Health</b>	IRES-3 (10:25)	IRES-3 (10:40)	IRES-3, SF-36 (40:54)	IRES-3, SF-36 (49:70)
<b>Pain</b>	SF-36, IRES-3 (15:19)	SF-36, IRES-3 (19:23)	IRES-3, SF-36 (40:54)	IRES-3, SF-36 (49:70)
<b>Mental Health</b>	IRES-3 (11:18)	IRES-3 (11:15)	IRES-3 (57:139)	IRES-3, SF-36 (43:57)

Note: Optimal sample sizes based on t-tests for dependent samples ( $\alpha=0.05$ ,  $\beta=0.20$ , Power=0.80, and observed standardized effect sizes, SRM)

# Limitations

- Representativeness of the **sample** (e.g. inclusion criteria, drop-out rate)
- Representativeness of **interventions and measurement points**
- Bias due to **effects of sequence** and **selective response patterns**
- **Comparability** of questionnaire scores
- Suitability of **descriptive and inferential statistical methods** (e.g. type I error, coefficients, tests...)
- **Practical aspects** (e. g. length, redundancy)

# Conclusion

- Sensitivity to change is an important concept in measurement theory.
- This criterion is especially relevant for intervention studies.
- Measurement instruments have to be compared in head-to-head studies, similar to intervention studies (RCTs).
- Generally speaking, the IRES-3 scores have equal or higher sensitivity to change than comparable scores of the SF-36 or the SCL-90-R.
- The observed differences in sensitivity to change can have dramatic consequences on optimal sample sizes in intervention studies.

*Thank you!*

Contact: [wilmar.igl@ki.se](mailto:wilmar.igl@ki.se)

# References

- Cronbach, L. J. (1957). The two disciplines of scientific psychology. *American Psychologist* 12, 671-684.
- Aiken, L. R. (2000). *Psychological Testing and Assessment* (10th ed.). Boston: Allyn and Bacon
- Rost, J. (2004). *Lehrbuch der Testtheorie – Testkonstruktion* [Textbook of test theory – test construction] (2. Aufl.). Bern: Huber.
- Terwee, C. B., Dekker, F. W., Wiersinga, W. M., Prummel, M. F. & Bossuyt, P. M. (2003). On assessing responsiveness of health-related quality of life instruments: Guidelines for instrument evaluation. *Quality of Life Research* 12, 349-362.
- Igl, W., Zwingmann, C. & Faller, H. (2006). Änderungssensitivität von Fragebogen zur Erfassung der subjektiven Gesundheit – Ergebnisse einer prospektiven vergleichenden Studie [Sensitivity to change of questionnaires measuring subjective health- results of a prospective comparative study]. *Rehabilitation* 45(4), 232-242.
- Igl, W. (2007). Änderungssensitivität und Responsivität von generischen Patientenfragebogen in der Rehabilitation [Sensitivity to change and responsiveness of generic patient questionnaires in rehabilitation]. Dissertation, Department of Psychology, Albert-Ludwigs-Universität Freiburg. Published at <http://www.freidok.uni-freiburg.de/volltexte/3015> on June 4, 2007.
- Bührlen, B., Gerdes, N. & Jäckel, W. H. (2005). Entwicklung und psychometrische Testung eines Patientenfragebogens für die medizinische Rehabilitation (IRES-3) [Development and psychometric testing of a patient questionnaire for medical rehabilitation (IRES-3), German Version]. *Rehabilitation* 44(2), 63-74.
- Bullinger, M. & Kirchberger, I. (1998). SF-36 Fragebogen zum Gesundheitszustand – Handanweisung [SF-36 Health Survey – Manual, German Version]. Göttingen: Hogrefe.
- Franke, G. H. (2002). SCL-90-R Symptom-Checkliste von L. R. Derogatis – Deutsche Version [SCL-90-R Symptom-Checklist by L. R. Derogatis – German Version] (2. Aufl.). Göttingen: Beltz.